

Lösungen lineare Gleichungen

1. Aufgabe

a)

$$\begin{array}{rcl} 14x - 3 & = & 9x + 12 \\ 14x & = & 9x + 15 \\ 5x & = & 15 \\ x & = & 3 \end{array} \quad \begin{array}{l} |+3 \\ |-9x \\ :5 \end{array}$$
$$L = \{3\}$$

b)

$$\begin{array}{rcl} -3x - 6 + x & = & 15 - 5x + 9 \\ -2x - 6 & = & -5x + 24 \\ -2x & = & -5x + 30 \\ 3x & = & 30 \\ x & = & 10 \end{array} \quad \begin{array}{l} |T \\ |+6 \\ |+5x \\ :3 \end{array}$$
$$L = \{10\}$$

c)

$$\begin{array}{rcl} -6x - 8 + 3x + 5 & = & -9x - 3 + 4x + 2 \\ -3x - 3 & = & -5x - 1 \\ 2x - 3 & = & -1 \\ 2x & = & 2 \\ x & = & 1 \end{array} \quad \begin{array}{l} |T \\ |+5x \\ |+3 \\ :2 \end{array}$$
$$L = \{1\}$$

d)

$$\begin{array}{rcl} -6x + 14 & = & 4(2x + 7) \\ -6x + 14 & = & 8x + 28 \\ -14x + 14 & = & 28 \\ -14x & = & 14 \\ x & = & -1 \end{array} \quad \begin{array}{l} |T \\ |-8x \\ |-14 \\ :(-14) \end{array}$$
$$L = \{-1\}$$

e)

$$\begin{array}{rcl} 19 - (6x + 6) & = & -2(2x - 5) - 3x \\ 19 - 6x - 6 & = & -4x + 10 - 3x \\ -6x + 13 & = & -7x + 10 \\ x + 13 & = & 10 \\ x & = & -3 \end{array} \quad \begin{array}{l} |T \\ |T \\ |+7x \\ |-13 \end{array}$$
$$L = \{-3\}$$

f)
$$\begin{aligned} 3(x+1)+x+5 &= -(x-10)+2x+4 & |T \\ 3x+3+x+5 &= -x+10+2x+4 & |T \\ 4x+8 &= x+14 & |-x \\ 3x+8 &= 14 & |-8 \\ 3x &= 6 & |:3 \\ x &= 2 \end{aligned}$$
 $L = \{2\}$

g)
$$\begin{aligned} 3(x+1)-(18-4x) &= 24-(2x-15) & |T \\ 3x+3-18+4x &= 24-2x+15 & |T \\ 7x-15 &= -2x+39 & |+2x \\ 9x-15 &= 39 & |+15 \\ 9x &= 54 & |:9 \\ x &= 6 \end{aligned}$$
 $L = \{6\}$